6.110 Quiz 2 (Spring 2025)

Before starting the quiz, write your name on this page and read the following instructions:

- There are 7 problems on this quiz. It is 18 pages long; make sure you have the whole quiz. You will have 50 minutes in which to work on the problems. You will likely find some problems easier than others; read all problems before beginning to work, and use your time wisely.
- The quiz is worth 50 points total. The point breakdown each problem is given in the table below, and is also printed with the problem. Some of the problems have several parts, so make sure you do all of them!
- This is an open-book quiz. You may use a laptop to access anything on or directly linked to from the course website, **except for Godbolt**. You may also use any handwritten notes. You **may not** use Godbolt, any compilers, the broader internet, any search engines, large language models, or other resources.
- Do all written work on the quiz itself. If you are running low on space, write on the back of the quiz sheets and be sure to write (OVER) on the front side. It is to your advantage to show your work we will award partial credit for incorrect solutions that are headed in the right direction. If you feel rushed, try to write a brief statement that captures key ideas relevant to the solution of the problem.

Problem	Title	Points
1	Dataflow Analysis	6
2	Register Allocation	13
3	Loop Analysis	6
4	Loop Optimization	6
5	Sign Information	10
6	Peephole Optimizations	8
7	Feedback	1
	Total	50

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1. Dataflow Analysis [6 pts]

Reaching definitions analysis determines which definitions of variable x reach any particular use of variable x. More formally, for any variable x, we say a definition D of x "reaches" the use U if:

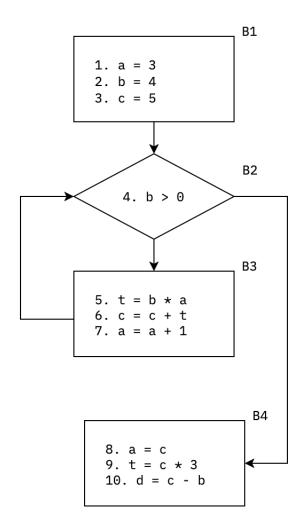
- *U* reads the value *x*
- There exists some path from *D* to *U* that does not redefine *x*.

Reaching definitions analysis is a forwards dataflow analysis performed using the following dataflow equations for each basic block *b*:

$$\mathsf{IN}[b] = \bigcup_{p \in \mathsf{pred}(b)} \mathsf{OUT}[p] \tag{1}$$

$$\mathsf{OUT}[b] = (\mathsf{IN}[b] \setminus \mathsf{KILL}[b]) \cup \mathsf{GEN}[b] \tag{2}$$

In this question, we will analyze the following program, where B1 is the entry block and B4 is the exit block.



(a) [2 pts] Fill in the following table with the GEN and KILL sets for each basic block. Write each set as a set of labels. Not all labels on the CFG have a corresponding definition. As a starting point, we have filled in the first row (B1) for you.

Block	GEN[B]	KILL[B]
B1	{1,2,3}	{6,7,8}
B2		
В3		
B4		

(b) [3 pts] For the following question, possible IN and OUT sets for block B3 is provided. For each possibility, first determine whether or not those sets could be a *valid* fixed-point solution to the dataflow analysis for the entire control graph. If not, say which dataflow equation, either (1) or (2), is violated.

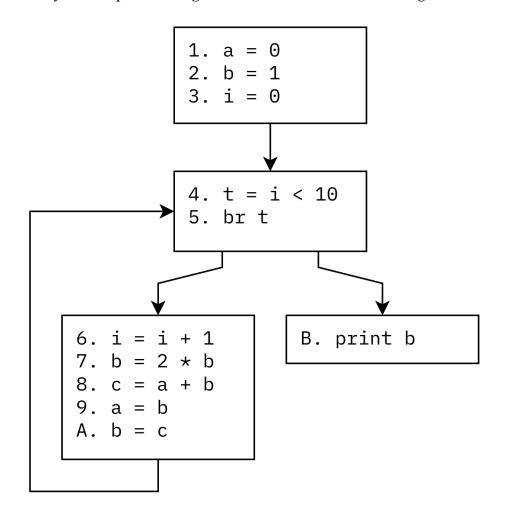
IN[<i>B</i> 3]	OUT[B3]	Valid/Invalid?	Violation ((1) or (2))
{1,2,3,5,6,7}	{2,5,6,7}		
{1,2,3,5,6,7,10}	{2,5,6,7,10}		
{2,3,5,6,7}	{2,5,6,7}		
{1,2,3,5,6,7,9}	{2,5,6,7,9}		

Note. The dataflow equations on page 2 of the exam are numbered (1) and (2).

Name	<u> </u>	Kerberos	4
	(c)	[1 pt] Would instruction 8 (a = c) be affected by copy propagation assuming other optimizations? Explain why or why not.	no

2. Register Allocation [13 pts]

In this problem, you will perform register allocation for the following CFG:



- (a) [5 pts] Identify all webs in the CFG above. Write each def/use as "<label>: def/use <variable>". A web has been given to you as an example.
 - Within each web, order the def/uses by ascending label number.
 - For webs of the same variable, order by the first label in ascending order.

There may be more rows than needed.

Web #	Variable	def-uses
1	t	4: def t, 5: use t
2	a	
3	a	
4	b	
5	b	
6	С	
7	С	
8	i	
9	i	

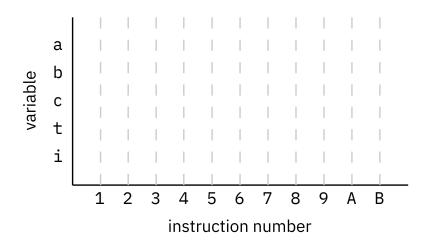
Kerberos __

Name _

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- (d) [3 pts] Now let's explore another way to do register allocation.
 - i. Assume we allocate registers to variables instead of webs;
 - ii. Assume instructions are ordered as follows: 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B;
 - iii. Assume a variable will be stored in the same register from its first use/def to the last use/def according to the order above.

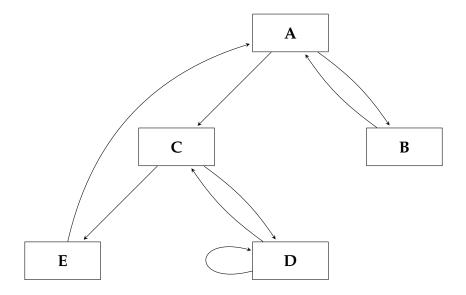
For each variable, draw a line segment in the figure below from its first def/use to its last def/use.



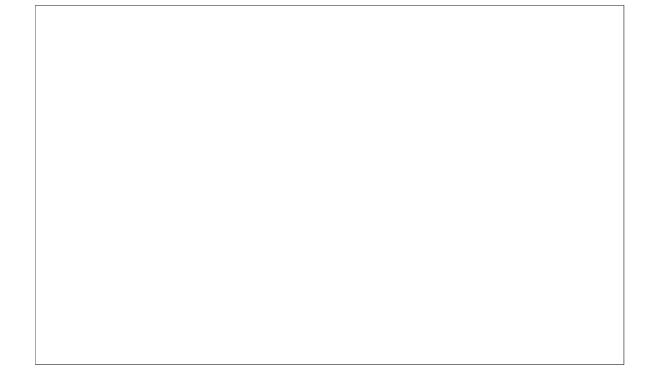
(e) [1 pt] What is the minimum number of registers needed by this register allocator?

3. Loop Analysis [6 pts]

Consider the following CFG. $\bf A$ is the entry block. Left arrows represent false branches, and right arrows represent true branches.



(a) [1 pt] Draw the dominator tree of this CFG.



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4. Loop Optimizations [6 pts]

Consider the following Decaf snippet.

```
int foo(int p) {
    int w, x, y, z;
    x = 0;
    while (x < 10) {
        z = 4 * x + 6;
        y = p * p + 100;
        w += foo(z) + y;
        x += 2;
    }
    return w;
}</pre>
```

(a) [2 pts] Identify any Base Induction Variables and Derived Induction Variables.

Variable	Base/Derived?	Induction Variable Triple

Name _	Kerberos 13
5. S i	gn Information [10 pts]
ca sil w ze	ppose we want to keep track of sign information for integer variables. Each variable in be either negative (Neg), zero (Zero), or positive (Pos). We represent the set of posble signs of a variable as a 3-bit vector , where the most significant bit (MSB) indicates nether the variable could be negative, the middle bit indicates if the variable could be ro, and the least significant bit (LSB) indicates if the variable could be positive. For ample:
	• Pos only \rightarrow 001
	• Zero only \rightarrow 010
	• Neg or Zero \rightarrow 110
(a) [2 pts] Draw the Hasse diagram for this lattice and define the join operator as an arithmetic or boolean operation. Hint : it should be a very simple operator.

(b) [4 pts] We define the lattice L for program variables x, y, and z, Each element $m \in L$ is a mapping:

$$m: \{x, y, z\} \rightarrow SignSets$$

where SignSets are subsets of $\{Neg, Zero, Pos\}$. Complete the following transfer function information:

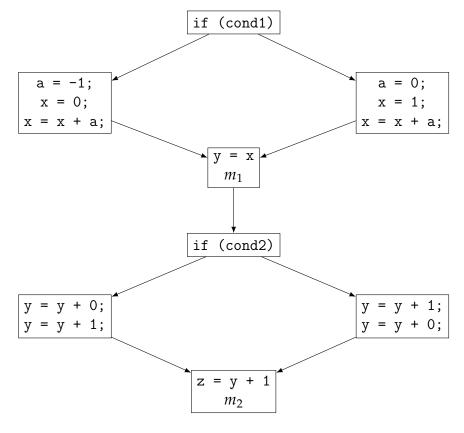
Operation	m(x)
x = -1	
x = 0	010
x = 1	001
x = y	

Additionally, complete the partial table for addition: if x and y have known signs, what is z = x + y?

x y	100	010	001
100	100		
010		010	
001			001
110			
111	111	111	111

Name_

Consider the following CFG where if (cond1) marks the entry block:



(c) [1 pt] m_1 is the mapping that the dataflow analysis computes for the program point aftery = x. What is $m_1(y)$?

(d) [1 pt] m_2 is the mapping that the dataflow analysis computes for the program point after z = y + 1. What is $m_2(z)$?

(e) [2 pts] How could one use sign set information to optimize code?

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6. Peephole Optimizations [8 pts]

Ben Bitdiddle has written a poorly optimized x86 code generator. Help him identify opportunities to make his assembly more performant. Make sure your optimized assembly is **semantically identical** to the left-hand side, and that it runs in **fewer cycles**, given the latency table below. Write your assembly code in AT&T syntax (source operand on the left), and make sure it is syntactically correct (i.e, an assembler would accept it). Assume a single-core, single-thread CPU executes one instruction at a time and in order.

Ben Bitdiddle downloads a latency table from a popular x86 reference website for Intel Skylake-X CPUs, which is the processor family on the 6.110 Derby Server:

	Operands	Latency		Operands	Latency		Operands	Latency
MOVQ	r/i,r	1	ADDQ SUBQ	r/i,r	1	SHLQ	i,r	1
MOVQ	r/i,m	2	ADDQ SUBQ	m,r	5	SHLQ	i,m	2
CMOVcc	r,r	1	CMPQ	r/i,r	1	SHRQ	i,r	1
XCHGQ	r,r	2	CMPQ	r/i,m	1	SHRQ	i,m	2
PUSHQ	r	3	IMULQ	r/m	3	SARQ	i,r	1
POPQ	r	2	IMULQ	r,r	3	SARQ	i,m	2
			IDIVQ	r	95			
			INCQ DECQ	r	1			
			INCQ DECQ	m	3			

Key: Operands: i (immediate), r (register), m (memory location).

Assembly	Optimized Assembly		
movq %r10, %rcx addq %r8, %r10 movq %r10, %rcx addq \$1, %r10 movq %r10, %rcx			
movq \$8, %r11 idivq %r11 movq %rax, %r10 movq \$0, %rdx			
movq \$32, %r11 imulq %r11, %r10			
<pre>shlq \$2, %rax addq %rcx, %rax movq (%rax), %rcx</pre>			

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7. Feed	lback [1	pt]						
(a)	[1 pt]	What is one thing you studied that did not show up on the exam?						
(b)	[0 pts]	[Optional]: Any other feedback for the course staff? (or feelzbox)						